

10.3 Quadratics in Standard Form

$$f(x) = \frac{-(-8)}{2(4)} = \frac{8}{8} = 1; \quad 4(1)^2 - 8(1) + 10$$

PRACTICE

$$f(x) = (1, 6); \quad g(x) \rightarrow (-4, -1)$$

Directions: Use the following functions to find the best answers for #1 - 3.

$$f(x) = 4x^2 - 8x + 10; \quad g(x) = 2(x+4)^2 - 1; \quad h(x) = (x+4)(x+2)$$

1) Which function has the lowest minimum value?

- a) f(x)
- b) g(x)
- c) h(x)
- d) g(x) and h(x)

2) Which function has the lowest y-intercept?

- a) f(x)
- b) g(x)
- c) h(x)
- d) f(x) and h(x)

3) Which function is the widest?

- a) f(x) because the leading coefficient is the greatest.
- b) g(x) because its in vertex form.
- c) h(x) because its leading coefficient is the smallest.
- d) They are all the same because they are all quadratics.

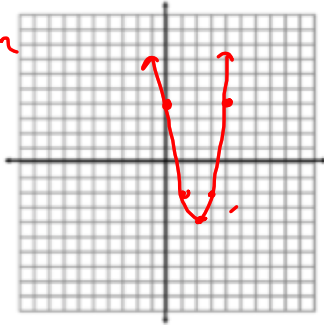
Directions: Graph each function. Then answer the questions. Plot the vertex and at least 2 other points, more if possible.

4) $f(x) = 2x^2 - 8x + 4$

Vertex: $x = \frac{-(-8)}{2(2)} = \frac{8}{4} = 2$
 $y = 2(2)^2 - 8(2) + 4 = 8 - 16 + 4 = -4$
 (2, -4)

Y-int: (0, 4)

X-ints (approx.): (0.5, 0) (3.5, 0)

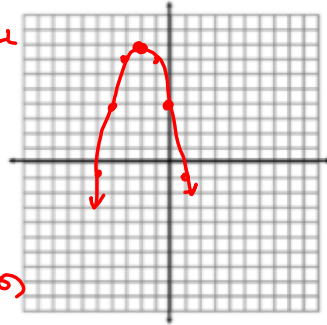


5) $f(x) = -x^2 - 4x + 4$

Vertex: $x = \frac{-(-4)}{2(-1)} = \frac{4}{-2} = -2$
 $y = -(-2)^2 - 4(-2) + 4 = -4 + 8 + 4 = 8$
 (-2, 8)

Y-int: (0, 4)

X-ints (approx.): (1.9, 0) (-4.9, 0)



6) $f(x) = -0.5x^2 + 5x - 6$

Vertex: $x = \frac{-5}{2(-0.5)} = \frac{-5}{-1} = 5$
 $y = -0.5(5)^2 + 5(5) - 6 = -12.5 + 25 - 6 = 6.5$
 (5, 6.5)

Y-int: (0, -6)

X-ints (approx.): (1.1, 0) (8.9, 0)

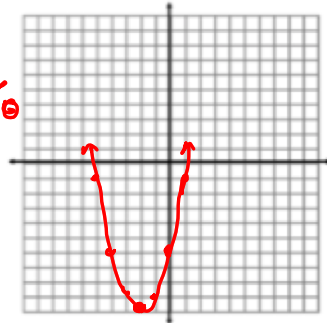


7) $f(x) = x^2 + 4x - 6$

Vertex: $x = \frac{-4}{2(1)} = \frac{-4}{2} = -2$
 $y = (-2)^2 + 4(-2) - 6 = 4 - 8 - 6 = -10$
 (-2, -10)

Y-int: (0, -6)

X-ints (approx.): (-5.1, 0) (1.1, 0)

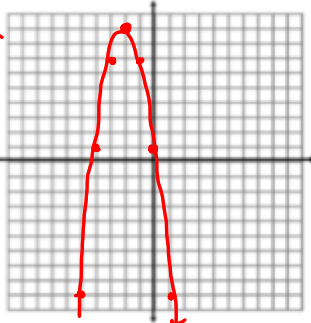


8) $f(x) = -2x^2 - 8x + 1$

Vertex: $x = \frac{-(-8)}{2(-2)} = \frac{8}{-4} = -2$
 $y = -2(-2)^2 - 8(-2) + 1 = -8 + 16 + 1 = 9$
 (-2, 9)

Y-int: (0, 1)

X-ints (approx.): (-4.1, 0) (1, 0)

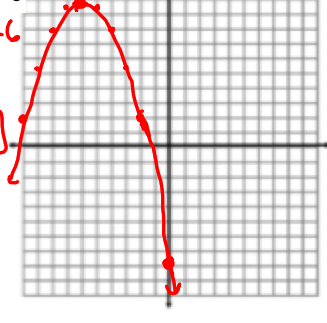


9) $f(x) = -0.5x^2 - 6x - 8$

Vertex: $x = \frac{-(-6)}{2(-0.5)} = \frac{6}{-1} = -6$
 $y = -0.5(-6)^2 - 6(-6) - 8 = -18 + 36 - 8 = 10$
 (-6, 10)

Y-int: (0, -8)

X-ints (approx.): (-10.1, 0) (-1.1, 0)

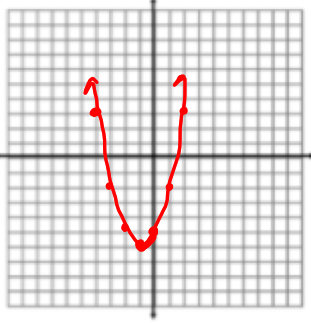


10) $f(x) = x^2 + 2x - 5$

Vertex: $x = \frac{-2}{2(1)} = \frac{-2}{2} = -1$
 $y = (-1)^2 + 2(-1) - 5 = 1 - 2 - 5 = -6$
 (-1, -6)

Y-int: (0, -5)

X-ints (approx.): (1.5, 0) (-3.5, 0)

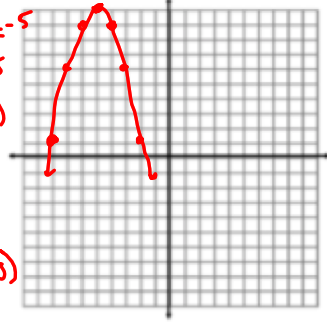


11) $f(x) = -x^2 - 10x - 15$

Vertex: $x = \frac{-(-10)}{2(-1)} = \frac{10}{-2} = -5$
 $y = -(-5)^2 - 10(-5) - 15 = -25 + 50 - 15 = 10$
 (-5, 10)

Y-int: (0, -15)

X-ints (approx.): (-1.9, 0) (-8.1, 0)



Directions 12-13: Solve each system.

12) $6x - 8y = -4$
 $4x + 2y = -10$
 $16x + 8y = -40$
 $6x - 8y = -4$

$$\begin{array}{r} 16x + 8y = -40 \\ 6x - 8y = -4 \\ \hline 22x = -44 \\ x = -2 \end{array}$$

$$\begin{array}{r} 4(-2) + 2y = -10 \\ -8 + 2y = -10 \\ 2y = -2 \\ y = -1 \end{array}$$

$(-2, -1)$

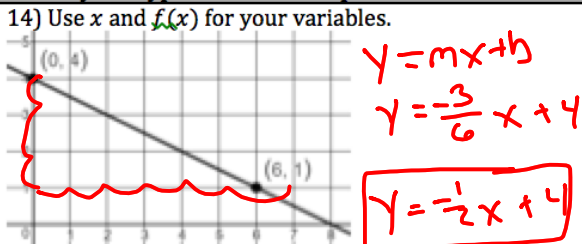
13) $2x + 8y = -16$
 $y = x - 12$

$$\begin{array}{r} 2x + 8(x - 12) = -16 \\ 2x + 8x - 96 = -16 \\ 10x - 96 = -16 \\ 10x = 80 \\ x = 8 \end{array}$$

$$\begin{array}{r} y = 8 - 12 \\ y = -4 \end{array}$$

$(8, -4)$

Identify the type of relationship and create a function from the given information.



15) There are 100 rodents in a barn. Every month m , the rodent population p increases by 200%.

$$100 \times 200 = 300$$

$y = a \cdot b^x$
 $y = 100(3)^x$

Determine whether each function has a maximum or minimum point and then find the value.

16) $f(x) = 3x^2 + 18x - 5$

MINIMUM VALUE @ $(-3, -32)$

$$x = -\frac{b}{2a} = -\frac{18}{2(3)} = -\frac{18}{6} = -3$$

$$y = 3(-3)^2 + 18(-3) - 5 = -32$$

17) $f(x) = -10x^2 - 200x + 100$

MAXIMUM VALUE @ $(-10, 1100)$

$$x = -\frac{b}{2a} = -\frac{200}{2(-10)} = -10$$

$$y = -10(-10)^2 - 200(-10) + 100 = 1100$$

18) $f(x) = -0.75x^2 + 33x - 5.5$

MAX VALUE @ $(22, 357.5)$

$$x = -\frac{b}{2a} = \frac{33}{2(-0.75)} = 22$$

$$y = -0.75(22)^2 + 33(22) - 5.5 = 357.5$$

19) $f(x) = 4000x^2 - 5$

MIN VALUE @ $(0, -5)$

$$x = -\frac{b}{2a} = 0$$

$$y = 4000(0)^2 - 5 = -5$$