

2.3 Solving Inequalities

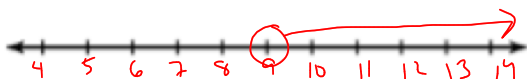
PRACTICE

Directions: Solve each inequality. Express the solution graphically and in set notation.

1) $7 < \frac{x}{9} + 6$

$$\begin{array}{r} -6 \quad -6 \\ (9) \mid < \frac{x}{9} \quad (9) \\ \hline 9 < x \end{array}$$

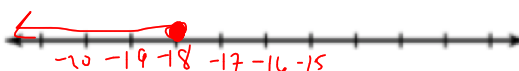
$$\{x \text{ real} \mid x > 9\}$$



2) $-7 + \frac{h}{3} \leq -13$

$$\begin{array}{r} +7 \quad +7 \\ (3) \frac{h}{3} \leq -6(3) \\ \hline h \leq -18 \end{array}$$

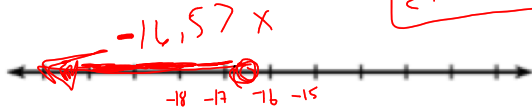
$$\{h \text{ real} \mid h \leq -18\}$$



3) $50.32 < -6.29(8.5 + x)$

$$\begin{array}{r} 50.32 < -53.465 + -6.29x \\ +53.465 \quad +53.465 \\ \hline 103.785 < -6.29x \\ -4.29 \quad -4.29 \\ \hline -16.57x \end{array}$$

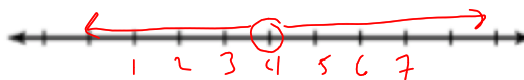
$$\{x \text{ real} \mid x < -16.57\}$$



4) $-3 - 3a + 6a \neq 9$

$$\begin{array}{r} -3 + 3a \neq 9 \\ +3 \quad +3 \\ \hline 3a + 12 \\ \hline a \neq 4 \end{array}$$

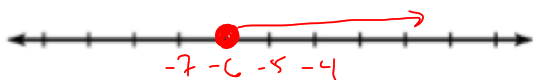
$$\{a \text{ real} \mid a \neq 4\}$$



5) $-5(1 - 2n) \geq -17 + 8n$

$$\begin{array}{r} -5 + 10n \geq -17 + 8n \\ -8n \quad -8n \\ \hline -5 + 2n \geq -17 \\ +5 \quad +5 \\ \hline 2n \geq -12 \\ \hline n \geq -6 \end{array}$$

$$\{n \text{ real} \mid n \geq -6\}$$

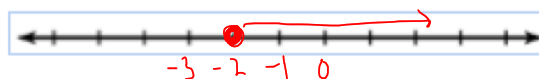


6) $30 - 4a \geq -2(7a - 5)$

$$\begin{array}{r} 30 - 4a \geq -14a + 10 \\ +14a \quad +14a \\ \hline 30 + 10a \geq 10 \\ -30 \quad -30 \\ \hline 10a \geq -20 \\ \hline a \geq -2 \end{array}$$

$$\begin{array}{r} 10a \geq -20 \\ \hline a \geq -2 \end{array}$$

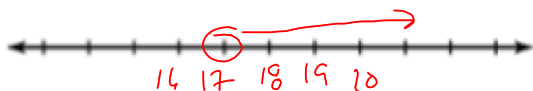
$$\{a \text{ real} \mid a \geq -2\}$$



7) $\frac{b+5}{22} > 1$ (22)

$$\begin{array}{r} b+5 > 22 \\ -5 \quad -5 \\ \hline b > 17 \end{array}$$

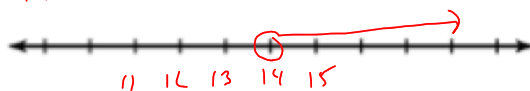
$$\{b \text{ real} \mid b > 17\}$$



8) $-36 > -3x + 6$

$$\begin{array}{r} -6 \quad -6 \\ -42 > -3x \\ \hline 14 < x \end{array}$$

$$\{x \text{ real} \mid x > 14\}$$



9) $11 \neq 2b - 1 - 6b$

$$\begin{aligned} 11 &\neq -4b - 1 \\ +1 & \\ \hline 12 &\neq -4b \\ \frac{-4}{-4} & \frac{-4}{-4} \\ -3 &\neq b \end{aligned}$$

$$\{b \text{ real} \mid b \neq -3\}$$

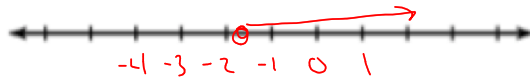


10) $-5.7x - 10.3 < 7.3x + 14.4$

$$\begin{aligned} -14.4 & \quad -14.4 \\ \hline -5.7x - 24.7 &< 7.3x + 14.4 \\ +5.7x & \quad +5.7x \\ \hline -24.7 &< 13x \\ \frac{-24.7}{13} & \quad \frac{13x}{13} \end{aligned}$$

$$-1.9 < x$$

$$\{x \text{ real} \mid x > -1.9\}$$

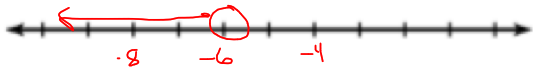


11) $16 + 4x \leq -4(x + 8)$

$$\begin{aligned} 16 + 4x &\leq -4x - 32 \\ +4x & \quad +4x \\ \hline 16 + 8x &\leq -32 \\ -16 & \quad -16 \\ \hline 8x &\leq -48 \\ \frac{8x}{8} &\leq \frac{-48}{8} \end{aligned}$$

$$x < -6$$

$$\{x \text{ real} \mid x < -6\}$$

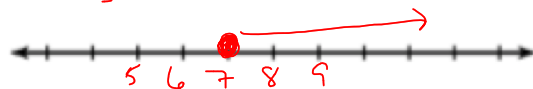


12) $-27 - 7h \geq -2h - (8h + 6)$

$$\begin{aligned} -27 - 7h &\geq -2h - 8h - 6 \\ -27 - 7h &\geq -10h - 6 \\ +10h & \quad +10h \\ \hline -27 + 3h &\geq -6 \\ +27 & \quad +27 \\ \hline 3h &\geq 21 \\ \frac{3h}{3} &\geq \frac{21}{3} \end{aligned}$$

$$h \geq 7$$

$$\{h \text{ real} \mid h \geq 7\}$$



Directions: Multiply the polynomials.

13) $2x(4x - 8)$

$$8x^2 - 16x$$

14) $(2x - 1)(4x - 8)$

$$8x^2 - 16x - 4x + 8$$

$$8x^2 - 20x + 8$$

15) $(2x - 1)(4x^2 - 8x + 3)$

$$8x^3 - 16x^2 + 6x - 4x^2 + 8x - 3$$

$$8x^3 - 20x^2 + 14x - 3$$