

## 9.4 Multi-Step Factoring

## PRACTICE

**Check the work!** Multiply out the factored form to see if it matches the polynomial.

1. Is  $2(x+6)(x-5)$  the factored form of  $2x^2 + 2x - 60$ ?

$$\begin{aligned} &2(x^2 - 5x + 6x - 30) \\ &\cancel{2}(x^2 + x - 30) \quad \text{YES!} \\ &2x^2 + 2x - 60 \quad \checkmark \end{aligned}$$

2. Is  $3x(x+4)^2$  the factored form of  $3x^3 + 48x$ ?

$$\begin{aligned} &3x(x+4)(x+4) \\ &3x(x^2 + 4x + 4x + 16) \\ &3x(x^2 + 8x + 16) \\ &3x^3 + 24x^2 + 48x \quad \times \end{aligned}$$

3. Is  $2d(d-7)(d-5)$  the factored form of  $2d^3 - 12d^2 - 35d$ ?

$$\begin{aligned} &2d(d^2 - 5d - 7d + 35) \\ &\cancel{2d}(d^2 - 12d + 35) \quad \text{NO!} \\ &2d^3 - 24d^2 + 70d \quad \times \end{aligned}$$

4. Is  $4(t+3)(t-3)$  the factored form of  $4t^2 - 36$ ?

$$\begin{aligned} &4(t^2 - 3t + 3t - 9) \\ &4(t^2 - 9) \\ &4t^2 - 36 \quad \checkmark \end{aligned}$$

**Factor the following if possible. Check your answer by multiplying!**

5.  $4x^2 - 20x - 144$

$$\begin{aligned} &4(x^2 - 5x - 36) \\ &\boxed{4(x-9)(x+4)} \quad \cancel{-5} \cancel{4} \\ &\quad \cancel{-9} \cancel{-36} \end{aligned}$$

**CHECK YOUR ANSWER!**

$$\begin{aligned} &4(x-9)(x+4) \\ &4(x^2 + 4x - 9x - 36) \\ &4(x^2 - 5x - 36) \\ &4x^2 - 20x - 144 \quad \checkmark \end{aligned}$$

6.  $m^3 - 4m$

$$\begin{aligned} &m(m^2 - 4) \\ &\boxed{m(m+2)(m-2)} \end{aligned}$$

**CHECK YOUR ANSWER!**

$$\begin{aligned} &m(m+2)(m-2) \\ &m(m^2 - 2m + 2m - 4) \\ &m(m^2 - 4) \\ &m^3 - 4m \quad \checkmark \end{aligned}$$

7.  $27x^2 + 45x$

$$\boxed{9x(3x+5)}$$

**CHECK YOUR ANSWER!**

$$\begin{aligned} &9x(3x+5) \\ &27x^2 + 45x \quad \checkmark \end{aligned}$$

8.  $2h^3 - 24h^2 + 40h$

$$\begin{aligned} &2h(h^2 - 12h + 20) \\ &\boxed{2h(h-2)(h-10)} \quad \cancel{-10} \cancel{-10} \\ &\quad \cancel{-8} \cancel{20} \end{aligned}$$

**CHECK YOUR ANSWER!**

$$\begin{aligned} &2h(h-2)(h-10) \\ &2h(h^2 - 10h - 2h + 20) \\ &2h(h^2 - 12h + 20) \\ &2h^3 - 24h^2 + 40h \quad \checkmark \end{aligned}$$

9.  $12t^2 - 27t - 27$

$$\begin{aligned} &3(4t^2 - 9t - 9) \quad \cancel{3} \cancel{-12} \\ &3(4t^2 + 3t - 12t - 9) \quad \cancel{-36} \\ &3[t(4t+3) - 3(4t+3)] \end{aligned}$$

**CHECK YOUR ANSWER!**

$$\begin{aligned} &3(t-3)(4t+3) \\ &3(4t^2 + 3t - 12t - 9) \\ &3(4t^2 - 9t - 9) \\ &12t^2 - 27t - 27 \quad \checkmark \end{aligned}$$

10.  $-4d^2 - 5d + 6$

$$\begin{aligned} &-(4d^2 + 5d - 6) \quad \cancel{-8} \cancel{-3} \\ &-[4d^2 + 8d - 3d - 6] \\ &-[4d(d+2) - 3(d+2)] \end{aligned}$$

**CHECK YOUR ANSWER!**

$$\begin{aligned} &-(4d-3)(d+2) \\ &-(4d^2 + 8d - 3d - 6) \\ &-(4d^2 + 5d - 6) \\ &-4d^2 - 5d + 6 \quad \checkmark \end{aligned}$$

**Solve the following by factoring.**

11.  $2x^2 + 28x - 64 = 0$

$$2(x^2 + 14x - 32) = 0$$

$$2(x+16)(x-2) = 0$$

$$2=0 \quad | \quad \begin{array}{l} x+16=0 \\ x-2=0 \end{array} \quad | \quad \begin{array}{l} x+2=6 \\ x-2=6 \end{array}$$

$$\cancel{x=-16} \quad \cancel{x=2} \quad | \quad \begin{array}{l} x=-16, 2 \\ x=2 \end{array}$$

12.  $0 = 5x^2 - 5$

$$0 = 5(x^2 - 1)$$

$$0 = 5(x+1)(x-1)$$

$$| \quad \begin{array}{l} x+1=0 \\ x-1=0 \end{array} \quad | \quad x-1=0$$

$$x=-1 \quad x=1$$

13.  $4x^3 - 12x^2 = -8x$

$$\cancel{4x^3} \quad \cancel{-12x^2} \quad \cancel{+8x}$$

$$4x^3 - 12x^2 + 8x = 0$$

$$4x(x^2 - 3x + 2) = 0$$

$$4x(x-2)(x-1) = 0$$

$$4x=0 \quad | \quad \begin{array}{l} x-2=0 \\ x-1=0 \end{array} \quad | \quad \begin{array}{l} x=0 \\ x=1 \end{array}$$

$$x=0 \quad x=2 \quad x=1$$

$$| \quad \begin{array}{l} x=0, 1, 2 \\ x=1 \end{array}$$

14.  $-p^2 = 11p + 18$

$$\cancel{-p^2} \quad \cancel{+11p} \quad \cancel{+18}$$

$$0 = p^2 + 11p + 18$$

$$0 = (p+2)(p+9)$$

$$| \quad \begin{array}{l} p+2=0 \\ p+9=0 \end{array} \quad | \quad \begin{array}{l} p=-2 \\ p=-9 \end{array}$$

$$p=-2 \quad p=-9$$

$$| \quad \begin{array}{l} p=-9, -2 \\ p=-9 \end{array}$$

15.  $15n^2 + 41n - 18 = 2n$

$$\cancel{15n^2} \quad \cancel{+41n} \quad \cancel{-18}$$

$$15n^2 + 39n - 18 = 0$$

$$3(5n^2 + 13n - 6) = 0$$

$$3(5n^2 - 2n^2 + 15n - 6) = 0$$

$$3(n(5n-2) + 3(5n-2)) = 0$$

$$3(n+3)(5n-2) = 0$$

$$| \quad \begin{array}{l} n+3=0 \\ n-2=0 \end{array} \quad | \quad \begin{array}{l} 5n-2=0 \\ 5n+2=0 \end{array}$$

$$n=-3 \quad \frac{n=2}{5}$$

$$| \quad \begin{array}{l} n=-3, \frac{2}{5} \\ n=\frac{2}{5} \end{array}$$

16.  $15x = 6x^3 - x^2 - 15x$

$$\cancel{15x} \quad \cancel{6x^3} \quad \cancel{-x^2} \quad \cancel{-15x}$$

$$0 = x(6x^2 - x - 15)$$

$$0 = x[6x^2 - 10x + 9x - 15]$$

$$0 = x[2x(3x-5) + 3(3x-5)]$$

$$0 = x(2x+3)(3x-5)$$

$$x=0 \quad | \quad \begin{array}{l} 2x+3=0 \\ 3x-5=0 \end{array} \quad | \quad \begin{array}{l} -3=-3 \\ 5=5 \end{array}$$

$$2x=-3 \quad 3x=5$$

$$x=-\frac{3}{2} \quad x=\frac{5}{3}$$

$$| \quad \begin{array}{l} x=-\frac{3}{2}, 0, \frac{5}{3} \\ x=\frac{5}{3} \end{array}$$

**Answer the following.**

17. Simplify  
 $(5x^2 - 2x) + (x^2 - x + 5)$   
 $5x^2 - 2x + x^2 - x + 5$   
 $\cancel{6x^2 - 3x + 5}$

18. Multiply  $(2x-1)^2$   
 $(2x-1)(2x-1)$   
 $4x^2 - 2x - 2x + 1$   
 $| \quad \begin{array}{l} 4x^2 - 4x + 1 \end{array}$

19. Solve  $\frac{4}{1} - \frac{1}{2}x = 8$   
 $(-\frac{2}{1}) - \frac{1}{2}x = 4(-\frac{2}{1})$   
 $x = -8$

20. Write the equation of the linear function for the situation below.  
Bob has 26 dollars and makes 5 dollars every 2 hours.

$$f(x) = 26 + \frac{5}{2}x$$

21. Write the equation of the exponential function for the situation.  
Bob has 26 dollars and triples his money every 2 weeks.

$$F(x) = 26(3)^{\frac{x}{2}}$$

22. If  $f(x) = 3x + 2$ , find  $f(3) + 4$   
 $f(3) = 3(3) + 2$   
 $f(3) = 11$

$$| \quad \begin{array}{l} -11+4 \\ -7 \end{array}$$